Abstract

Data collection path planning is a problem to determine a cost-efficient path to read the most valuable data from a given set of sensors. The problem can be formulated as a variant of the combinatorial optimization problems that are called the price-collecting traveling salesman problem or the orienteering problem in a case of the explicitly limited travel budget. In these problems, each location is associated with a reward characterizing the importance of the data from the particular sensor location. The used simplifying assumption is to consider the measurements at particular locations independent, which may be valid, e.g., for very distant locations. However, measurements taken from spatially close locations can be correlated, and data collected from one location may also include information about the nearby locations. Then, the particular importance of the data depends on the currently selected sensors to be visited by the data collection path, and the travel cost can be saved by avoiding visitation of the locations that do not provide added value to the collected data. This is a computationally challenging problem because of mutual dependency on the cost of data collection path and the possibly collected rewards along such a path. A novel solution based on unsupervised learning method called the Growing Self-Organizing Array (GSOA) is proposed to address computational challenges of these problems and provide a solution in tens of milliseconds using conventional computational resources. Moreover, the employed GSOA-based approach allows to exploit capability to retrieve data by wireless communication or remote sensing, and thus further save the travel cost.

Keywords: Unsupervised learning, Data-Collection Planning, Spatial Correlations, GSOA

1. Introduction

Autonomous data collection is a problem studied in robotics in which one or several robotic vehicles are requested to collect the most valuable sensor measurements from a given set of sensors in a cost-efficient way or even with an explicitly limited travel budget. The problem is motivated by several practical scenarios such as data retrieving from pre-deployed sensor networks [1] to study ocean floor [2, 3], monitoring algae blooms [4], volcanic activity [5, 6], and pollution monitoring [7] or environment monitoring missions [8]. The problem is to determine a cost-efficient path to visit a set of sensor locations that can be formulated as the combinatorial Traveling Salesman Problem (TSP) [9], which is known to be NP-hard unless P=NP [10].

Data from a sensor can be remotely retrieved using wireless communication [11], and thus a precise visitation of the sensor locations can be avoided to save the travel cost. Such an extension of the TSP is called the TSP with Neighborhoods (TSPN) or with explicitly specified disk-shaped neighborhoods for a symmetric communication range δ as the Close Enough TSP (CETSP) [12], e.g., used in forest fire detection in [13]. Since for δ = 0 the problem becomes the TSP, also the TSPN is NP-hard.
Solving the TSPN (or CETSP) optimally is computationally very demanding, e.g., using Mixed Integer Non-linear Programming [14], and thus heuristic approaches [15, 16] and evolutionary techniques have been proposed [17] including unsupervised learning approaches [18, 19]. Besides, the CETSP can be addressed by an explicit sampling of the possible locations within the particular disk-shaped neighborhood around each sensor location, and the problem can be solved as the Generalized TSP (GTSP) [20] using heuristic approaches [21, 22]. The main drawback of this sampling-based approach is that the size of the problem is quickly increasing for a simple sampling strategy and a solution of such a transformed problem is computationally demanding [23].

In addition to the challenges related to the remote sensing or data retrieving within the $\delta$ range [24], another important part of data collection planning is the fact that the quality of data retrieved from each sensor can be characterized as expected information received. Therefore, it may be suitable to avoid visitation of sensors that provide less important data in a benefit of reducing the travel cost or collecting more rewarding data from a distant location. This aspect can be considered in formulation of the data collection planning as the Prize-Collecting TSP (PCTSP) [25], i.e., extended to the PCTSP with Neighborhoods (PCTSPN) [26], or the Orienteering Problem (OP) [27, 28] that has been relatively recently generalized into the OP with Neighborhoods (OPN) [29, 30, 31].

In the PCTSP, each sensor has associated a penalty if data from the sensor are not collected and the problem is to determine a path such that the sum of the path length and sum of the penalties for not visiting sensors is minimal. For the OP, each sensor has associated reward for the retrieved data from it, but the main difference is that the length of the data collection path maximizing the sum of the collected rewards has to not exceed the given travel budget $T_{\text{max}}$ [27].

Both the PCTSPN and OPN formulations can be utilized for planning a data collection path to retrieve data from the most rewarding sensors; however, in most of the existing approaches (further described in Section 2), the measurements are considered independent, and thus also the rewards associated to the sensors are fixed, i.e., the reward (penalty) value of the particular sensor does not depend on the collected data from other sensors. Although such an assumption may hold for many practical cases, there are also problems where the collected data are used for modeling and predicting large-scale and spatially correlated environment phenomena [32]. In such a case, the solution becomes more challenging as the reward values depend on the currently selected sensors to be visited by the data collection path.

In this paper, the data collection planning with spatially correlated measurements is addressed. The proposed solution originates from the previous successful deployment of unsupervised learning methods in the solution of the PCTSPN [33], OPN [31], and early results on the PCTSPN with spatial correlations reported in [34]. However, a novel unsupervised learning procedure for routing problems called the Growing Self-Organizing Array (GSOA) [19] is employed in the presented approach to solving the close enough variants of the PCTSP and OP with spatially correlated measurements. Since the presented work originates in the previous approaches, the particular contributions are considered as follows:

- Generalization of the GSOA for the CETSP [19] to the solution of the Close Enough PCTSP (CEPCTSP)
- and its further extension to the problems with spatially correlated measurements.
- Novel GSOA-based solution of the Close Enough Orienteering Problem (CEOP)
- with comparison to the previous unsupervised learning based approaches;
- and its application to problems with spatially correlated measurements.
Beside of that, the herein proposed approach is the first deployment of the GSOA [19] in the solution of the orienteering problems. Specifically, the proposed GSOA-based solver provides competitive solutions to the previous unsupervised learning based approaches to the OP, it improves the solution quality in the CEOP, and it is also capable to exploit spatial correlation of the measurements. Thus, the presented GSOA approach provides solution of the whole class of the data collection planning problems including CETSP, CEPCTSP, OP, and CEOP all with spatially correlated measurements.

The remainder of the paper is organized as follows. An overview of the related work on the PCTSP, OP, and also correlated measurements is presented in the following section. Formulations of the addressed problems together with the model of the spatial correlations are in Section 3. The proposed GSOA-based solutions of the Close Enough PCTSP and OP are presented in Section 4 and results on their evaluations and comparisons with existing approaches are reported in Section 5. Finally, Section 6 is dedicated to the concluding remarks.

2. Related Work

Two main problem formulations can be found in the literature to solve data collection path planning, the Prize-Collecting TSP (PCTSP) [25] and the Orienteering Problem (OP) [27]. Both problem formulations can be extended to their variants with the neighborhoods and also spatial correlations. An overview of the existing approaches is presented in this section to provide a context and emphasize the main challenges.

Existing approaches for the PCTSP include approximate algorithms [35, 36] and unsupervised learning technique [37]. The PCTSPN extends the problem to determine the particular locations where the data are retrieved from the sensors, which allows exploiting retrieving data remotely from the sensors. Authors of [26] address the PCTSPN by a decoupled approach that combines heuristics to determine locations inside the respective neighborhood of the sensors and a solution of the standard TSP to find the path connecting the locations. A unifying approach based on unsupervised learning has been presented in [33] which directly addresses the continuous space of the neighborhood of each sensor. Despite the approach [33] does not utilize the explicit sampling of the neighborhood into a pre-specified discrete set as [26], it is less computationally demanding, and it provides significantly better solutions.

Even though the PCTSPN can be used for planning data collection paths, the main drawback of this formulation is the question how to balance the trade-off between the path length and the sum of penalties for not visited sensors. There is a single objective function in the PCTSP formulation in which the total solution cost is the sum of the travel cost (the path length) and the penalties for not visited sensors, e.g., see Problem 3.1. If the balance is not easy to setup, it may be more suitable to formulate the data collection planning problem as the OP or as the OPN to exploit a non-zero communication range δ.

Many approaches and variants of the OP have been proposed in the literature [38, 28]. On the other hand, an explicit solution of the OPN has been introduced relatively recently and the first such a solution is based on the unsupervised learning techniques [29, 30, 31, 39]. Besides, the Variable Neighborhood Search (VNS) meta-heuristic [40] can be utilized for sampled neighborhoods into discrete sets, but such a solution is computationally very demanding.

Probably the first approach directly addressing the spatially correlated measurements in data collection planning has been proposed in [41]. The authors formulate the data collection planning problem on a discrete graph, where rewards are associated with the nodes of the graph and the rewards may be related to the neighborhood nodes.
The problem is called the Correlated Orienteering Problem (COP), and the proposed solution is based on Mixed Integer Quadratic Programming (MIQP). The reported results are for graphs formed as a grid with up to $12 \times 12$ nodes for which solutions are found in tens or hundreds of seconds using Intel Core-i7 5820 CPU [41].

Another recent approach addressing the data collection planning with spatially correlated measurements is based on unsupervised learning technique previously employed in the solution of the PCTSPN [34]. The authors exploit low computationally requirements of [33] and update the reward values during the learning. The influence of visiting one location to the rewards (penalties) of the neighboring locations are considered in a continuous space, contrary to the discrete model of [41]. The rewards (penalties) are updated based on the idea that measurements from one or several locations may also include information about the measurements at the nearby locations.

In [34], it is assumed that the influence of spatial correlations is decreasing with the distance of the sensor locations and from a specific distance, the measurements are not correlated at all. The spatial correlation is therefore formulated as a distance based model of correlation between the sensor measurements. The actual value of the reward is determined online from the default value of the reward $r$ (without the influence of the other sensors) proportionally decreased by the ratio computed from the geometrical relations of the neighboring sensors using the so-called correlation radius $\chi$ and reward (penalty) radius $\xi$ of the involved sensors.

Performance of the method proposed in [34] is demonstrated in the same PCTSPN scenario as in [33], further denoted as the OOI, and the reported computational requirements are in tens of milliseconds using similar computational resources as in [41] but with utilizing only a single core of the CPU. The solution cost is a bit improved if spatial correlations are considered in comparison to the previous approach [33]; however, with increasing communication range $\delta$, such a benefit is less noticeable.

The MIQP-based approach [41] is formulated on a discrete graph where the travel cost from one location to another location is a weight of the particular edge. On the other hand, the unsupervised learning method [34] is considered in the continuous space which provides an advantage of determining suitable locations for collecting the rewards during the solution of the problem; and the travel cost is directly computed as the Euclidean distance between two respective locations. However, the unsupervised learning can be deployed on a graph [42] and the Euclidean distance can be replaced by point-to-point path planning using a motion planning roadmap [43] at the cost of more complex and more demanding algorithm. Besides, an artificial potential field has been used as a navigation function in [44], and therefore, similar approaches such as [45] can be eventually utilized.

Here, it is worth mentioning that the learning techniques employed in [33] and [31] have been consolidated and conceptually simplified into unifying unsupervised learning based approach for solving routing problems in [19]. The novel method is called the Growing Self-Organizing Array (GSOA). Even though the GSOA originates from the SOM-based approaches for the TSP, one of its main advantages is that it directly supports the selection of the most rewarding sensors in the data collection planning problems with an adjustment of the number of learning nodes, contrary to SOM-based approaches that require a fixed number of neurons defined prior the learning, e.g., see [46, 47, 48]. Besides, it does not need explicit parameter tuning.

In [19], the GSOA is evaluated and compared with other state-of-the-art SOM-based solvers for the regular TSP in representative benchmarks of the TSPLIB [49], where it provides the best trade-off between the solution quality and the required computational time. Moreover, the GSOA has also been evaluated and compared in the solution of the CETSP instances where it provides competitive or better results than the heuristic approaches, but it is about three orders of magnitude faster than a heuristic based on a solution of the related GTSP [19]. Another
advantage of the GSOA is its flexibility to solve CETSP instances with individual communication radius per each sensor, and thus it supports local properties of the sensors surroundings and communication capabilities of each sensor.

Based on the overview of the existing approaches and results reported therein, the GSOA is considered as the promising approach to address data collection planning with spatially correlated measurements in a new unifying way. Further, motivated by the evaluation presented in [19], the PCTSPN and OPN are rather called the Close Enough PCTSP (CEPCTSP) and Close Enough OP (CEOP) to emphasize the disk-shaped neighborhoods of the sensors. Therefore, the GSOA is applied in the solution of the CEPCTSP and CEOP with spatially correlated measurements using the geometrical model of the spatial correlations proposed in [34]. The particular formulations of the problems addressed in this paper are presented in the following section.

3. Problem Statement and Formulations

The data collection planning addressed in this paper is formulated as two problems that can be found in the literature, the Prize-Collecting Traveling Salesman Problem (PCTSP) and Orienteering Problem (OP) both considered in their close enough variants to exploit capability to retrieve data from the sensors within the communication range \( \delta \), and thus save the travel cost. Besides, both problems are considered with spatially correlated measurements that may influence the associated rewards (penalties) to the sensors if data from the nearby sensors are retrieved along the data collection path being found. The problems are formally introduced in the following paragraphs, but the model of spatial correlation is addressed separately (in Section 3.1) to make the problem definitions clear and readable as it only changes the way how the rewards are computed.

Both the problem formulations share the description of the data collection mission that consists of the set of \( n \) sensors \( S \) located in a plane, \( S \subset \mathbb{R}^2 \). The position of each sensor \( s_i \) is known and for simplicity and with a slightly overloaded notation, the sensor location is denoted \( s_i \) and \( S = \{s_1, \ldots, s_n\} \), i.e., \( s_i \in \mathbb{R}^2 \). The data collection vehicles are operating in \( \mathbb{R}^2 \) with a constant average velocity. The travel cost \( c(p_1, p_2) \) between \( p_1 \in \mathbb{R}^2 \) and \( p_2 \in \mathbb{R}^2 \) can be directly computed from the Euclidean distance between \( p_1 \) and \( p_2 \) and it is assumed w.l.o.g. \[ c(p_1, p_2) = \| (p_1, p_2) \|. \]

In the original formulation of the PCTSP [25], it is considered that each sensor \( s_i \) has associated penalty \( \zeta(s_i) \geq 0 \), while rewards \( r(s_i) \geq 0 \) are considered in the OP [27]. The herein presented formulation of the PCTSP is slightly modified to unify the symbols and notation of the PCTSP and the OP. The penalties \( \zeta(s_i) \) are considered as the rewards \( r(s_i) \), but since the sum of penalties is combined with the travel cost in the PCTSP, it is necessary to scale the reward value to the penalty and \( \zeta(s_i) = \lambda r(s_i) \) and w.l.o.g., \( \lambda = 1 \) is considered to simplify the notation.

In the rest of the paper, \( r_i \) is used instead of \( r(s_i) \) whenever it is clear the reward is associated with the \( i \)-th sensor \( s_i \).

In planning a data collection path, we are searching for a subset of \( k \) sensors \( S_k \subseteq S \) from which the most rewarding data are collected along the cost-efficient path. Therefore, the data collection path can be specified by a permutation \( \Sigma_k \) defining the order of visits to the sensors \( S_k \), and \( \Sigma_k \) is a permutation of the sensor labels \( \Sigma_k = (\sigma_1, \ldots, \sigma_k) \), where \( 1 \leq \sigma_i \leq n \) and \( \sigma_i \neq \sigma_j \) for \( i \neq j \).

Having these preliminaries and not considering the communication range, i.e., \( \delta = 0 \), the PCTSP can be formulated as Problem 3.1. W.l.o.g. the vehicle starting location is considered to be the sensor location \( s_1 \), i.e., \( \sigma_1 = 1 \), and it is always selected to be in \( S_k \).
Problem 3.1 (PCTSP – Prize-Collecting TSP).

\[
\begin{align*}
\min_{1 \leq k \leq n, S_k \subseteq S} & \quad C(S_k, \Sigma_k) \\
C(S_k, \Sigma_k) & = \sum_{i=1}^{k-1} \| (s_{\sigma_i}, s_{\sigma_{i+1}}) \| \\
& + \| (s_{\sigma_k}, s_{\sigma_1}) \| \\
& + \lambda \sum_{s_j \in S \setminus S_k} r(s_j)
\end{align*}
\]

\[
\begin{align*}
\text{s.t.} & \quad 1 \leq k \leq n; \quad 1 \leq \sigma_i \leq n; \quad \sigma_i \in \Sigma_k \\
& \quad s_{\sigma_i} \in S_k; \quad s_{\sigma_1} = s_1; \quad s_1 \in S_k
\end{align*}
\]

The term (3) is because the PCTSP follows the TSP where the requested path has to be closed, and the term (4) represents the sum of penalties for not visited sensors.

For the Close Enough PCTSP (CEPCTSP), it is allowed to retrieve data from \( s_i \) within the range \( \delta_i \). Therefore, the problem is not only to determine the subset \( S_k \) of \( k \) sensors and the order of visits \( \Sigma_k \) to minimize the cost function \( C(S_k, \Sigma_k) \), but also the most suitable waypoint locations \( P = \{ p_{\sigma_1}, \ldots, p_{\sigma_k} \} \), \( p_i \in \mathbb{R}^2 \) are requested to be found such that \( \| (p_i, s_i) \| \leq \delta_i \). Hence, the CEPCTSP is not a purely combinatorial problem as the PCTSP, and it includes a continuous optimization part as the particular waypoint can be arbitrarily selected within the distance \( \delta_i \) from the respective sensor location \( s_i \).

Problem 3.2 (CEPCTSP – Close Enough PCTSP).

\[
\begin{align*}
\min_{1 \leq k \leq n, S_k \subseteq S, \Sigma_k, \mathbf{p}_k \subseteq \mathbb{R}^2} & \quad C(S_k, \Sigma_k, \mathbf{p}_k) \\
C(S_k, \Sigma_k, \mathbf{p}_k) & = \sum_{i=1}^{k-1} \| (p_{\sigma_i}, p_{\sigma_{i+1}}) \| \\
& + \| (p_{\sigma_k}, p_{\sigma_1}) \| \\
& + \lambda \sum_{s_j \in S \setminus S_k} r(s_j)
\end{align*}
\]

\[
\begin{align*}
\text{s.t.} & \quad 1 \leq k \leq n; \quad 1 \leq \sigma_i \leq n; \quad \sigma_i \in \Sigma_k \\
& \quad s_{\sigma_i} \in S_k; \quad s_{\sigma_1} = s_1; \quad s_1 \in S_k \\
& \quad p_{\sigma_i} \in \mathbf{P}_k; \quad \| (p_{\sigma_i}, s_{\sigma_i}) \| \leq \delta_i
\end{align*}
\]

Notice, we assume the initial location of the vehicle is \( s_1 \), and therefore, it may be suitable to set \( \delta_1 = 0 \). The communication radius can be individual per each sensor; however, a single \( \delta \) is used in the rest of the paper whenever the radii are considered the same to simplify the notation.

The OP is similar to the PCTSP in selecting the most rewarding sensors, but it differs in explicitly prescribed travel budget and maximizing the total collected rewards. Besides, the original formulation [27] specifies the initial and final locations of the data collection vehicle which are w.l.o.g. defined as \( s_1 \) and \( s_n \), both with the zero rewards.
$$r_1 = r_n = 0.$$ The OP is combinatorial optimization problem to select \(k\) sensors \(S_k \subseteq S\) with the maximal sum of the rewards such that the length of the path connecting them (that starts at \(s_1\) and terminates at \(s_n\)) does not exceed the travel budget \(T_{\text{max}}\). Thus, at least two sensors are selected\(^1\) in \(S_k\), i.e., \(k \geq 2\) and \(\sigma_1 = 1\) and \(\sigma_k = n\). The OP is formally defined as Problem 3.3.

**Problem 3.3 (OP – Orienteering Problem).**

$$\max_{k, S_k \subseteq S, \Sigma_k} R(S_k, \Sigma_k) = \sum_{i=1}^{k} r(s_{\sigma_i})$$

subject to

$$\sum_{i=1}^{k-1} \| (s_{\sigma_i}, s_{\sigma_{i+1}}) \| \leq T_{\text{max}}$$

$$\Sigma_k = (\sigma_1, \ldots, \sigma_k); \quad 2 \leq k \leq n$$

$$1 \leq \sigma_i \leq n; \quad \sigma_1 = 1; \quad \sigma_k = n$$

$$s_{\sigma_i} \in S_k; \quad s_{\sigma_1} = s_1, \quad s_{\sigma_k} = s_n$$

Similarly to the CEPCTSP, the waypoints \(P_k\) at which data from the selected sensors are retrieved are determined in the Close Enough OP (CEOP), where we consider \(\delta_1 = \delta_n = 0\) as it is requested to start and finish the mission exactly at the locations \(s_1\) and \(s_n\), respectively, and thus \(p_1 = s_1\) and \(p_k = s_n\). The CEOP is formally defined as Problem 3.4.

**Problem 3.4 (CEOP – Close Enough OP).**

$$\max_{k, S_k \subseteq S, \Sigma_k, P_k} R(S_k, \Sigma_k, P_k) = \sum_{i=1}^{k} r(s_{\sigma_i})$$

subject to

$$\sum_{i=1}^{k-1} \| (p_{\sigma_i}, p_{\sigma_{i+1}}) \| \leq T_{\text{max}}$$

$$\Sigma_k = (\sigma_1, \ldots, \sigma_k); \quad 2 \leq k \leq n$$

$$1 \leq \sigma_i \leq n; \quad \sigma_1 = 1; \quad \sigma_k = n$$

$$s_{\sigma_i} \in S_k; \quad s_{\sigma_1} = s_1, \quad s_{\sigma_k} = s_n$$

$$\| (p_{\sigma_i}, s_{\sigma_i}) \| \leq \delta_{\sigma_i}; \quad p_1 = s_1; \quad p_k = s_n$$

### 3.1. Model of Spatially Correlated Sensor Measurements

A distance-based model of the spatially correlated measurements has been presented in [30]; however, it is briefly described here to make the paper self-contained. The main idea of the model is that the value of the reward (penalty) characterizing the possible information gain of the collected data from a particular sensor \(s_i\) depends on how much data from the nearby sensors are collected. Thus, including a particular sensor in the selected subset \(S_k\) may decrease rewards of the nearby sensors from \(S_k \setminus S_k\).

In general, data are collected to study some spatial or even spatiotemporal phenomena that can be modeled as a time-varying scalar field, \(\Psi(p, t), p \in \mathbb{R}^2\) [41]. Having the sampled data at the sensor locations \(S\), the problem is to create a model of the field from the collected values \(\Psi(s_i, t)\) at the particular sensor locations \(s_i \in S\). In [41],

\(^1\)It is assumed the travel budget \(T_{\text{max}}\) is at least \(T_{\text{max}} \geq \| (s_1, s_n) \|\) otherwise a feasible solution does not exist.
the authors model the spatial relations in a graph $G(V, E)$ where $V$ denotes the sensors and $G(V, E)$ has an edge $(v_i, v_j)$ if and only if $\Psi(v_j, t)$ is dependent on $\Psi(v_i, t)$, i.e., measurements at corresponding sensor locations $s_j$ and $s_i$, respectively. $\Psi(v_i, t)$ can have a form

$$
\Psi(v_i, t) = f_i(\Psi(v_{i_1}, t), \ldots, \Psi(v_{i_l}, t)),
$$

where $N_i = \{v_{i_1}, \ldots, v_{i_l}\}$ are the neighboring sensors of $v_i$ in the graph $G(V, E)$.

Having a subset of the selected sensors $S_k$ with the corresponding subset $V_k \subseteq V$, the quality of the field model created from the collected data $\Psi(v_i, t)$ for $v_i \in V_k$ can be computed as the reward function $J : \{S_k\} \rightarrow \mathbb{R}^+ \cup \{0\}$ that maps data from the sensors $S_k$ to real values [41]. The contribution of measurements from a sensor $s_i$ can be then expressed as

$$
J_{S_k}(s_i) = J(S_k \cup \{s_i\}) - J(S_k).
$$

(13)

Using (13), we can compute the default reward $r(s_i)$ considering $S_k = \emptyset$. Then, during the solution of the PCTSP or OP, the reward value of the sensors not included in the currently selected $S_k$ can be updated, i.e., $r(s_i) = J_{S_k}(s_i)$.

Despite the fact that the formulas (12) and (13) provide a general way how to compute the rewards, its particular evaluation depends on the phenomena studied from the collected measurements. Therefore the distance-based model of the spatial correlations has been proposed in [34] to evaluate benefits of considering spatial correlations in the solution of the PCTSP in a phenomenon independent way. In this paper, we follow this model which is summarized in the rest of this section.

![Figure 1: Geometrical relations of the correlation and penalty radii in the utilized distance-based model of the spatial correlations proposed in [34].](image)

Each sensor location $s_i \in S$ is associated with the default reward $r(s_i)$ and two radii defining two circles centered at $s_i$ that are called the correlation radius $\chi(s_i)$ and reward radius $\xi(s_i)$ (formerly the penalty radius in [34]). The circles are further referred as the correlation circle and reward circle with the particular radii $\chi(s_i)$ and $\xi(s_i)$, respectively. The geometrical relations of the radii are depicted in Fig. 1, where the default reward $r(s_i)$ of the sensor $s_i \notin S_k$ is decreased according to the influence of the data collected from the sensors $s_j, s_{j+1} \in S_k$. The
influence is computed as the union of the covered parts of the reward circle of \( s_i \) by the correlation circles of the sensors \( s_j \) and \( s_{j+1} \).

Let the total circumference of the reward circle with the radius \( \xi(s_i) \) be \( \text{circ}(\xi(s_i)) \), the selected sensors be \( S_k \), the neighboring sensors of the sensor \( s_i \in S_k \) in the graph \( G(V,E) \) be \( N_i \), and the default reward of \( s_i \) be \( r(s_i) \). The reward of \( s_i \) can be decreased because of correlation with the data provided by the sensors \( N_i \) that are collected by the current data collection path. The updated value of \( r(s_i) \) with respect to \( S_k \) is determined as

\[
r_{S_k}(s_i) = \left( 1 - \frac{L(\xi(s_i), N_i \cap S_k)}{\text{circ}(\xi(s_i))} \right) r(s_i),
\]

where \( L(\xi(s_i), N_i \cap S_k) \) is the length of the union of covered parts of the reward circle \( \xi(s_i) \) by the correlations circles of the influencing sensors selected in \( S_k \), i.e., circles of the sensors \( s_j \in N_i \cap S_k \) with the radii \( \chi(s_j) \) centered at \( s_j \).

Individual values of the correlation and reward radii (circles) can be set for each particular sensor. The model (14) can be then utilized during the solution of the PCTSP and OP to update the rewards of all sensors not currently selected in \( S_k \) whenever \( S_k \) is changed. The objective functions of the PCTSP and CEPCTSP, i.e., (1) and (5), respectively, include penalties (scaled values of the rewards) only for the sensors in \( S \setminus S_k \). Since the rewards of \( S_k \) are not considered, it is not necessary to make any adjustments in the formulations of Problem 3.1 and Problem 3.2. The only needed calculation is the sum of penalties that can be influenced by the data collected from the selected \( S_k \) because of (14).

The sums of rewards in the OP (8) and CEOP (10) are computed using only the sensors \( S_k \) selected for data collection. Therefore, it is necessary to include the model (14) into the solution cost \( R(S_k) \) as the sum of the total collected rewards should also include the rewards collected as a result of the spatial correlation of \( S_k \) to \( S \setminus S_k \), and thus the objective function \( R(S_k) \) is computed as

\[
R(S_k) = \sum_{s_i \in S_k} r(s_i) + \sum_{s_j \in S \setminus S_k} (r(s_j) - r_{S_k}(s_j)),
\]

where \( r_{S_k}(s_j) \) is computed according to (14). Notice, when \( \chi(s_i) \) is zero for all the sensors, the second term of (15) is zero and the spatial correlation between the measurements is not considered.

4. GSOA-based Data Collection Path Planning

The herein studied data collection path planning is addressed by the GSOA [19] which is a variant of the unsupervised learning network based on the principles of self-organizing map (SOM) for the TSP. The GSOA is an array of nodes \( \mathcal{N} = \{\nu_1, \ldots, \nu_M\} \) that represents points in the problem space, i.e., \( \nu \in \mathbb{R}^2 \). The connected nodes form a ring which represents the requested data collection path that evolves during the unsupervised learning of the GSOA. Each node \( \nu \in \mathcal{N} \) is further associated with the particular sensor \( \nu \cdot s \) and the corresponding waypoint location \( \nu \cdot p \) at which data from \( s \) can be retrieved within \( \delta \) communication radius, i.e., the waypoint location is inside the \( \delta \)-disk centered at \( s \). A similar notation as for the sensors is used for the nodes, and \( \nu \) denotes the node, and its location is \( \nu \).

The learning procedure is an iterative adaptation of the GSOA to the sensors \( S \) in a finite number of learning epochs. In each learning epoch, a new node \( \nu^* \) may be added to \( \mathcal{N} \) for each sensor \( s \in S \) and \( \nu^* \) can be then adapted towards \( s \). The sensors \( S \) are considered in a random order for each learning epoch to avoid local optima. For each sensor \( s \) a new node \( \nu^* \) is determined together with the waypoint location \( \nu^* \cdot p \) using the winner node
selection, see Fig. 2a. Then, $\nu^*$ together with its neighbouring nodes in the ring are adapted towards the waypoint location $\nu^*, p$, i.e., their positions are adjusted to “move” towards the waypoint

$$\nu' = \nu + \mu f(\sigma, d)(\nu^* - \nu)$$

with the power of the adaptation defined by the neighbouring function

$$f(\sigma, d) = \begin{cases} e^{-\frac{d^2}{\sigma^2}} & \text{for } d < 0.2M \\ 0 & \text{otherwise} \end{cases},$$

where $M$ is the current number of nodes in $N$ and $d$ is the distance of the node $\nu$ from $\nu^*$ in the number of nodes in the ring. Finally, all non-winning nodes are removed from $N$ at the end of each learning epoch to keep the number of nodes in $N$ balanced with the number of sensors.

![Diagram](image.png)

**Figure 2:** Demonstration of the principle of winner node selection (on the left) where the closest point of the ring of connected nodes $N$ to the particular sensor $s_5$ is determined as the position of the new node $\nu^*$ together with the particular waypoint $p$ to retrieve data from $s_5$ within $\delta$ communication range. (on the right) The ring of nodes $N$ defines the order of visits to the sensors associated with the nodes and the connected waypoints $p$ form the requested data collection path that is shown in red. The nodes are shown as small blue disks, and the sensor locations are shown as small green disks with the particular surrounding perimeter according to the communication range $\delta$. The images are adapted from [19] where the GSOA for the CETSP is introduced.

The array of nodes $N$ represents a ring in $\mathbb{R}^2$ and the sequence of nodes in the ring defines the order of visits to the sensors associated with the nodes. Moreover, the sequence of nodes defined by the array $N$ and the associated waypoint locations to the nodes can be used to quickly construct the data collection path from which data from the selected sensors can be retrieved. This is the main benefit of the GSOA over the SOM-based solvers for the TSP because it allows to trade-off the visitation of the particular sensor and the path length in a solution of the PCTSP or to explicitly address the limited travel budget in the OP. Besides, the growing structure allows to easily adjust the number of nodes according to the selected sensors. The winner selection and an example of the path represented by the ring are depicted in Fig. 2. Note that in the GSOA, a feasible solution is available at the end of
each learning epoch, and therefore, there are no issues with the convergence, and the GSOA has anytime property, see detailed discussion in [19].

The GSOA as it has been introduced for solving the TSP and CETSP in [19] can be almost directly used in the solution of the CEPCTSP and CEOP. There are two main adjustments needed to solve these problems. The first is the initialization of the ring $\mathcal{N}$, where the ring is initialized to a single node located at $s_1$, which is the same as for the TSP; however, an open path with the initial location $s_1$ and terminal location $s_n$ is requested in the OP. Therefore, the GSOA is initialized as two nodes $\nu_1$ and $\nu_{end}$ that are never adapted nor removed from the array. Besides, the neighboring function (17) has to respect the open path in the solution of the OP and CEOP.

The second adjustment is related to trade-off the path length and rewards of the not visited sensors in the PCTSP and to satisfy the budget limit $T_{max}$ in the OP. Both these aspects are addressed by the same way as the conditional adapt of the GSOA to the particular sensors. New nodes are determined for all sensors in every learning epoch, but the new node is inserted into the GSOA only if certain criteria are met. In the case of the PCTSP, the adaptation is performed only if the distance of the new node $\nu^*$ and its waypoint location $\nu^*,p$ is shorter than the penalty (reward) to not collect data from $s$, i.e., the adaptation is performed only if $\| (\nu^*,\nu^*,p) \| \leq \lambda r(\nu^*,s)$. However, for the first learning epoch, it is likely the case that new nodes are very far from the sensors, and thus this rule is not active for the first learning epoch.

For the OP, the adaptation of the ring is performed only if the path represented by the ring after the adaptation would be shorter than $T_{max}$ [31]. Because the nodes in $\mathcal{N}$ have associated waypoints, this can be evaluated as follows. Let the current epoch be $i$, the current ring $\mathcal{N}$ have $M$ nodes and represent a path with the length $L$, $\nu^*$ be the current winner node, $\nu_{prev}$ be the first neighboring node of $\nu^*$ in the direction to $\nu_1$ that has been added to $\mathcal{N}$ in the epoch $i$ (or $\nu_1$ if such a node has not been added yet), and $\nu_{next}$ be similarly the first neighboring node of $\nu^*$ towards $\nu_M$ added in the current epoch (or $\nu_{end}$ if such a node has not been added yet), then $\nu^*$ is kept in $\mathcal{N}$ and the ring is adapted towards the respective sensors only if

$$L - d_p(\nu_{prev},\nu_{next}) + d_p(\nu_{prev},\nu^*) + d_p(\nu^*,\nu_{next}) \leq T_{max},$$

where $d_p(\nu_i,\nu_j)$ is the distance between the waypoints associated to $\nu_i$ and $\nu_j$, i.e.,

$$d_p(\nu_i,\nu_j) = \| (\nu_i,p,\nu_j,p) \|. \quad (19)$$

If the conditional adaptation is not performed, the new node $\nu^*$ is discarded and the ring is not adapted towards the particular $s$.

Beside of these conditions for the actual adaptation of the nodes to the particular sensor location, it is desirable to consider the rewards associated with the sensors. In [31], it is proposed to adjust the power of adaptation (16) according to the reward of the sensor towards which the ring is adapted. This is especially suitable for solving instances of the OP, where the preference of highly rewarding sensors is crucial in finding high-quality solutions. Therefore, the adaptation has the form

$$\nu' = \nu + R(s)\mu f(\sigma,d)(\nu^*,p-\nu), \quad (20)$$

where $R(s)$ is the normalized reward of the sensor $s$ computed as $R(s) = r(s)/R_{max}$ for

$$R_{max} = \max_{s \in S} r(s). \quad (21)$$

The value of the sensor reward $r(s)$ is a subject of change when spatial correlations are considered, but since the learning is performed in several iterations, the updated rewards can be directly utilized whenever the network is
Figure 3: Evolution of the GSOA in a solution of the CEPCTSP with spatial correlations. The nodes are visualized as small light blue disks connected to the ring. The sensors are shown as colored disks where sensors with high rewards (penalties) are in red and sensors with low rewards are in blue. The final solution is the data collection path connecting the waypoints shown as small orange disks. The red segments connecting waypoints with the sensors denote the communication range $\delta$. The spatial correlations are shown by connecting the influencing sensors by green segments. Thus each sensor $s_i$ from which data are directly collected are connected with the $N_i$ neighboring nodes that are not selected in the solution, but a part of the information about the locations is included in data collected from $s_i$.

adapted to the sensors, and the sensor is selected to be part of the data collection path for the current learning epoch.

The adaptation (20) is beneficial for solving the OP, but it does not provide an added value in a solution of the PCTSP. Although it negligibly increases the solution cost, according to the performed evaluations it increases computational cost noticeably because of slower convergence, and therefore, the standard adaptation (16) is rather
Learning epoch 50

Learning epoch 163

Learning epoch 460

Final found solution

Figure 4: Evolution of the GSOA in a solution of the CEOP instance called Set 66 with the travel budget $T_{\text{max}} = 60$, communication range $\delta = 1.0$, and $\chi = 0$, i.e., without the spatial correlations. The visualization follows the same color schema as in Fig. 3. A new solution is determined every learning epoch, and therefore, the GSOA is performing as a stochastic search where the best solution found so far is maintained during the learning.

preferred for solving the PCTSP.

In addition to the conditional adaptation, it is suggested in [31] to support adaptation by avoiding saturation of the path length close to $T_{\text{max}}$ and up to two nodes of $\mathcal{N}$ may be removed from the array if the length of the path represented by the array would be longer than $T_{\text{max}}$ after adding new sensor to $S_k$. These two nodes represent the node $\nu_f \in \mathcal{N}$ with the longest distance to its waypoint $\nu_f.p$ and the node $\nu_l \in \mathcal{N}$ which is the node associated to the sensor $\nu_l.s$ with the lowest reward. Both the nodes $\nu_f$ and $\nu_l$ can be therefore removed from $\mathcal{N}$ during the winner node selection. However, if the ring is not adapted to the sensor because of (18), the deletion of these nodes is rolled-back, i.e., the ring is set to the state before the winner node selection.

Examples of the proposed GSOA for data collection planning in a solution of the CEPCTSP with spatial correlations is shown in Fig. 3. The solution follows the GSOA for the CETSP [19], and the network quickly converges to a stable solution which does not evolve with further learning epochs. Thus, solutions of the CEPCTSP instances reported in Section 5 are found in tens of learning epochs and typically in less than one hundred epochs. An example of the GSOA evolution in solving the CEOP instance Set 66 is presented in Fig. 4.

An overview of the GSOA learning procedure is depicted in Fig. 7 where the particular modifications to solve PCTSP and OP formulations of the data collection path planning algorithms are highlighted. The additional procedure for removing nodes $\nu_f$ and $\nu_l$ in solving instances of the OP is depicted in Fig. 6.
Figure 5: Evolution of the relative solution cost (sum of the rewards) in particular learning epochs to the final solution cost in solving the Set 66 instance of the OP and CEOP with $T_{\text{max}} = 60$ for $\delta = 0$ and $\delta = 1$, respectively.

**Procedure** remove_nodes($\mathcal{N}, s, \nu^*$):

1. Get all winner nodes of the current epoch $\mathcal{N}_{\text{win}} \leftarrow \text{winners}(\mathcal{N} \setminus \lbrace \nu_1, \nu_{\text{end}} \rbrace)$.
2. Determine the winner node $\nu_f$ which has the longest distance to its associated waypoint $\nu_f.p$
   \[ \nu_f = \arg\max_{\nu \in \mathcal{N}_{\text{win}}} \| (\nu, \nu.p) \|. \quad (22) \]
3. Determine the winner $\nu_l$ which associated sensor location $\nu_l.s$ has the lowest reward
   \[ \nu_l = \arg\min_{\nu \in \mathcal{N}_{\text{win}}} r(\nu.s). \quad (23) \]
4. If the expected path length after the adaptation of $\nu^*$ would be longer than $T_{\text{max}}$.
   - If $r(\nu_f.s) < r(s) \land \| (\nu_f, \nu_f.s) \| > \| (\nu^*, s) \|$ Then remove $\nu_f$ from the ring $\mathcal{N} \leftarrow \mathcal{N} \setminus \lbrace \nu_f \rbrace$.
   - If $r(\nu_l.s) < r(s) \land \| (\nu_l, \nu_l.s) \| > \| (\nu^*, s) \|$ Then remove $\nu_l$ from the ring $\mathcal{N} \leftarrow \mathcal{N} \setminus \lbrace \nu_l \rbrace$.
5. return($\mathcal{N}$).

Figure 6: Removing of not promising nodes from the current ring to support adaptation of the current winner node $\nu^*$ and satisfying the limited travel budget $T_{\text{max}}$ in a solution of the OP. The procedure has been originally proposed in [31].

A new solution is determined in every learning epoch in solving the OP. It is because new nodes are added to the ring for every considered sensor which is selected according to (18). Since only the newly added nodes in the current learning epoch are preserved for the next epoch, and sensors are evaluated in a random order, the learning procedure can be considered as a stochastic search. However, it is not an issue as the best solution found so far is maintained (Line 25 of the GSOA algorithm depicted in Fig. 7) and it can only improve over the time. An evolution of the solution cost (the sum of the collected rewards $R$) found in the particular learning epochs and the final best-found solution are depicted in Fig. 5. It can be noticed that a solution close to the final solution is found relatively quickly in around 200 learning epochs, but a bit better solution can be found in additional epochs. Because the computational requirements of the GSOA are relatively very low, see the results reported in Section 5, the maximal number of learning epochs is set to $i_{\text{max}} = 500$. The initial values of the learning parameters are set at Line 2 of the GSOA algorithm in Fig. 7. The particular values have been found empirically and they originate from the evaluation reported in [50]. Although the performance of the GSOA can be tuned by adjusting the parameters’
GSOA for data collection planning formulated as the Close Enough PCTSP and OP

Input: $S = \{s_1, \ldots, s_n\}$ – a set of sensor locations to be visited, each with particular disk-shaped $\delta$-neighborhood and default reward value $r_i$. For the spatially correlated measurements, each sensor $s_i \in S$ is further associated with the correlation radius $\chi_i$ and reward radius $\xi_i$.

Input: $T_{max}$ – the maximal allowed travel budget in the case of solving the OP.

Input: $i_{max}$ – the maximal number of learning epochs, i.e., $i_{max} \leftarrow 150$ for solving the PCTSP and $i_{max} \leftarrow 500$ for solving the OP.

Output: $(S_k, \Sigma_k, P_k) - S_k$ is a set of $k$ selected sensors, $\Sigma_k$ is the order of visits to the sensors, $P_k$ is the array of the corresponding waypoint locations at which data from $S_k$ can be retrieved.

1. **Initialization**
2. Set the learning parameters: the initial value of the learning gain $\sigma \leftarrow 10$, the gain decreasing rate $\alpha \leftarrow 0.0005$, and the learning rate $\mu \leftarrow 0.6$.
3. **if solving the PCTSP**: $N' \leftarrow \{v_1\}$ such that $v_1 = s_1$; $v_1$ is always adapted towards $s_1$ in every learning epoch.
4. **if solving the OP**: $N' \leftarrow \{v_1, v_{end}\}$ such that $v_1 = s_1$, $v_{end} = s_n$, and $v_1$ and $v_{end}$ are never changed nor removed from $N$ during the learning.
5. $i_{max} \leftarrow \min(i_{max}, 1/\alpha)$ \hspace{1cm} // ensure $\sigma$ will always be above 0
6. $i \leftarrow 1$ \hspace{1cm} // set the learning epoch counter
7. while $i \leq i_{max}$ and solution is changing do
8.   **Learning epoch**
9.   foreach $s$ in a random permutation of $S$ do
10.      $\nu' (\nu', \nu^*; p) \leftarrow \text{determine_winner}(N', s, \delta_i)$ \hspace{1cm} // Determine the winner node for $s$ according to Fig. 2
11.    **if solving the PCTSP** then
12.       $N' \leftarrow N$ \hspace{1cm} // save the ring for the case the adaptation would fail because of $T_{max}$
13.       $N' \leftarrow \text{remove_nodes}(N', s, \nu^*)$ \hspace{1cm} // remove nodes to possibly fit the path length to $T_{max}$, see Fig. 6
14.    **Conditional adapt**
15.       if $\big( (i = 1) \lor (\| (\nu^*, \nu; p) \| \leq \lambda r(s) ) \big)$ \hspace{1cm} \text{Condition (18) holds}
16.          $N' \leftarrow \text{insert_winner}(N, \nu^*)$ \hspace{1cm} \text{for solving the PCTSP}
17.          $N' \leftarrow \text{insert_winner}(N, \nu^*)$ \hspace{1cm} \text{for solving the OP}
18.       else
19.          $\text{Adapt } \nu \text{ towards } \nu^*; p \text{ using (16) for solving the PCTSP or using (20) for solving the OP with the neighborhood function (17)}.
20.      end
21.    **Update the ring and the best solution found so far**
22.       $N' \leftarrow \text{regenerate}(N)$ \hspace{1cm} // remove all not winning nodes from $N$
23.       $i \leftarrow i + 1$ \hspace{1cm} // update the epoch counter
24.       $\sigma \leftarrow (1 - \eta) \sigma$ \hspace{1cm} // decrease the learning gain
25. Determine a solution $S'_k$ and $\Sigma'_k$ with the corresponding waypoints $P'_k$ by traversing the current ring of nodes. If
26. \hspace{1cm} $C(S'_k, \Sigma'_k, P'_k) < C(S_k, \Sigma_k, P_k)$ \hspace{1cm} \text{for solving the PCTSP}
27. \hspace{1cm} $R(S'_k, \Sigma'_k, P'_k) > R(S_k, \Sigma_k, P_k))$ \hspace{1cm} \text{for solving the OP}
28. \hspace{1cm} $(S_k, \Sigma_k, P_k) \leftarrow (S'_k, \Sigma'_k, P'_k)$ \hspace{1cm} // update the best solution found so far
29. return $(S_k, \Sigma_k, P_k)$

Figure 7: An overview of the GSOA for solving the PCTSP and OP; both also in the Close Enough variant as the CEPCTSP and the CEOP. For the solution of the OP, nodes $v_f$ and $v_l$ can be removed from the ring using the remove_nodes($N', s, \nu^*$) procedure that is depicted in Fig. 6.

values, the performance is only slightly changing, and therefore, they are considered as constants.

Also note that for small budgets $T_{max}$ it does not make sense to consider sensor locations that are unreachable. Therefore, sensors for which $T_{max}$ does not allow to travel from $s_1$ and returning to $s_n$ are not considered in the
solution of the particular OP instance, similarly to heuristic approaches, e.g., 4-phase algorithm [51].

5. Results

The proposed GSOA for data collection path planning has been evaluated in a series of scenarios where the data collection planning problem is addressed as one of the variants of the PCTSP and OP. The performance of the GSOA in solving the PCTSP is performed in the OOI scenario that has been introduced in [33], which is motivated by autonomous data collection from a set of 128 sampling stations located on an ocean floor. Several instances of the PCTSP and CEPCTSP are created from the OOI scenario also considering correlations between the sensors. An example of two instances with visualization of the spatial correlations and individual communication radius per each sensor are depicted in Fig. 8.

On the other hand, scenarios used for evaluation of the GSOA in OP instances are created from the standard benchmarks proposed in [52]. In particular, the problems called Set 64 and Set 66 are considered because they represent more complex problems than the other standard OP benchmarks available at [53]. In addition to these existing benchmarks, the OOI scenario utilized in the evaluation of the PCTSP [33] and visualized in Fig. 8 is considered for creation of new OP instances with the two additional locations for the requested initial and terminal position of the vehicle with the total number of locations 130. The original OOI scenario is proportionally scaled down about the factor 10 to make it close to the standard Set 64 and Set 66, and the new OP dataset is called Set 130\(^2\). Each OP scenario is further defined by the particular value of the travel budget \(T_{\text{max}}\) (see [53] or the further reported results),

\(^2\)The OP instances of the Set 130 are available at https://purl.org/faigl/op.
Figure 9: Instances of the OP scenarios Set 64 and Set 66 both with the reward radius $\xi = 0.5$, the correlation radius $\chi = 2$, and the identical communication radius for all the sensors $\delta = 0.5$. The green line segments denote nearby correlated sensors.

where for increasing budget, more sensors can be visited and the problem can be considered closer to the TSP. The newly introduced Set 130 is accompanied with the travel budget $T_{\text{max}} = \{50, 100, 150, 200, 250, 300, 350, 400, 410\}$. The problems are also used to create instances of the CEOP with particularly specified communication radii $\delta$.

An example of the particular instances of the Set 64 and Set 66 with communication radius $\delta = 0.5$ is depicted in Fig. 9 to show the dimensions of the problem and spatial relations. Besides, selected instances are further used in evaluation of spatial correlations that is studied for different values of the correlation radius $\chi$ and reward radius $\xi$. Influence of different correlation radii to the influencing nearby sensors in Set 64 scenarios with zero communication radius is demonstrated in Fig. 10. An overview of the Set 130 is visualized in solutions shown in Fig. 21 and Fig. 22.

The PCTSP also with the non-zero communication radius $\delta$ as the CEPCTSP have been already addressed by the unsupervised learning together with the comparison with traditional combinatorial heuristics in [54,33] and with spatial correlations firstly tackled in [34]. Thus, the herein presented evaluation results on the PCTSP is mainly to show the influence of different correlation radii and performance of the GSOA in solving this type of data collection planning formulation.

The focus of the presented performance evaluation is on the novel GSOA-based approach to the OP and CEOP.
together with the study of the influence of spatial correlations to the sum of the collected rewards to demonstrate the capability of the proposed GSOA solution to exploit the non-zero communication radius and correlation radius. The first SOM-based unsupervised learning approach to the CEOP has been presented in [30] and its improved version in [31] together with the comparison to the existing combinatorial heuristics in the standard OP benchmarks [53]. Therefore, the proposed GSOA solution is compared with the approaches [30] and [31] that are further denoted as SOM v1 and SOM v2, respectively. Besides, the results in standard OP instances are compared with one of the best performing traditional heuristic [52] denoted as the CGW and one of the very first heuristics for the OP called 4-phase [51] that has been reimplemented to compare computational requirements of the combinatorial heuristic with unsupervised learning based approaches. Since the only existing available solvers for the CEOP without spatial correlations are those based on unsupervised learning, the performance evaluation is presented for selected CEOP instances. Finally, the only currently available solution for the CEOP with spatial correlations is the proposed GSOA-based method, and thus the evaluation is focused on the study the influence of the correlation radius and communication radius to the solution cost and computational requirements.

The used parameters of the SOM-based solvers are set as they are reported in [30] and [31]. For the proposed GSOA-based solvers the same values of the initial learning gain $\sigma$, the gain decreasing rate $\alpha$, and the learning rate $\mu$ as presented in Fig. 7 are used for both problems: the PCTSP and OP. The only difference is that for solving the PCTSP, the maximal number of learning epochs is set to $i_{max} = 150$ because the network usually converges in tens of epochs. For the solution of the OP, $i_{max}$ is set to $i_{max} = 500$ as the learning is de facto stochastic search.

All the unsupervised learning and 4-phase [51] algorithms have been implemented in C++ and run within the same computational environment using a single core of the Intel Core i7-6700K processor running at 4 GHz. The SOM-based and GSOA-based algorithms are stochastic, and therefore, the presented results are computed from 20 trials per each particular problem instance that is defined by the scenario, reward, correlation, and communication radii and in the case of the OP also the travel budget $T_{max}$.

The performance indicators are the solution quality and the required computational time. The solution quality is reported as the average cost of the solution $C$ (accompanied by the standard deviation) for the PCTSP instances. In the case of the OP, the solution quality is reported as the average collected sum of the rewards $R$ that is rounded to integers as the rewards are integer values in Set 64 and Set 66 [53]. Besides, following the literature on the OP [55, 56], the quality is also reported as the relative percentage error (RPE) computed as

$$\text{RPE} = \frac{R_{opt} - R}{R_{opt}} \cdot 100\%,$$

where $R$ is the best solution among the performed trials and $R_{opt}$ is the optimal solution for the particular instance reported in the literature [56, 57, 28] and also found by the ILP-based solver for the OP. Besides, the algorithm robustness over the performed trials is reported as the average relative percentage error (ARPE) [56]

$$\text{ARPE} = \frac{R_{opt} - R_{avg}}{R_{opt}} \cdot 100\%,$$

where $R_{avg}$ is the average sum of the collected rewards among the trials of the particular problem instance. For the newly introduced Set 130, the best solution found among of all evaluated algorithms is considered as the reference solution $R_{ref}$ instead of $R_{opt}$ because the optimal solution is not available.

The required computational time $T_{CPU}$ is reported as the average real computational time that is presented in milliseconds due to the computational efficiency of the proposed GSOA and unsupervised learning approaches. The standard deviations are shown as error bars in the accompanied bar plots.
5.1. Close Enough PCTSP with Correlation Measurements

The performance of the proposed GSOA in the PCTSP instances, or more particularly in the CEPCTSP instances with spatial correlations, has been evaluated in OOI scenarios with different communication and correlation radii. The selected OOI scenarios represent data collection missions from an area about 450×700 km large performed by an autonomous underwater vehicle operating with a constant velocity 5 km/h [33]. The communication range $\delta$ is considered up to 20 km, i.e., $\delta \in \{0, 5, 10, 20\}$ in km, the reward radius $\xi = 25$ km, and the correlation radius is considered as $\chi \in \{0, 14, 35\}$ in km.

![Figure 11: The average solution cost per each OOI scenario of the PCTSP with spatially correlated rewards (penalties) for the communication radius $\delta$ and correlation radius $\chi$. The reward radius $\xi$ of the distant based spatial correlation model is $\xi = 25$ km; however, the spatial correlations are enabled only for $\chi > 0$.](image)

The average solution cost is depicted in Fig. 11a. It can be noticed that the increasing communication range $\delta$ has a significant positive influence on the solution cost. However, the benefit of exploiting spatial correlations is mostly noticeable for $\delta = 0$ and $\chi = 35$ km. The average computational requirements per solution of a single trial are depicted in Fig. 11b. In all cases, the solution is provided in less than one hundred milliseconds. The computational requirements are slightly increased with increasing communication range $\delta$ but from a certain distance, the convergence of the network is faster, and thus the learning needs less number of learning epochs. Regarding the spatial correlations, the learning procedure is noticeably more demanding for increased $\chi$. It is because for a longer $\chi$ more sensors are in the influencing neighborhood set $N_i$ and the evaluation of (14) is more computationally intensive.

For the particular case of the evaluated OOI scenarios, considering spatial correlations only slightly decreases the solution cost. In particular, for $\delta = 0$ the average solution cost $C$ is $C = 841$ km for $\chi = 0$ km and it is $C = 790$ km for $\chi = 35$ km, which is noticeable but not directly visible in Fig. 11a. On the other hand, considering $\delta = 5$ km and $\chi = 0$ km, the average solution cost is significantly lower $C = 724$ km. Nevertheless, the proposed GSOA approach is capable of exploiting the spatial correlations between the measurements in benefit of the improved solution at the cost of increased computational requirements, which are about two times more demanding for $\chi = 35$ km than for $\chi = 0$ km.

5.2. GSOA in the Orienteering Problem

The performance of the novel GSOA-based solution of the OP has been evaluated using the standard OP benchmarks Set 64 and Set 66 [53] with 64 and 66 nodes, respectively, and with the travel budget $T_{\text{max}}$ ranging
from 15 to 80 and 130, respectively. The detail results are presented in Table 1 and Table 2. Besides, the OP instances for the Set 130 have been solved by the implemented 4-phase [51] heuristics and the unsupervised learning based approaches, and the results are reported in Table 3.

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<td>2.80</td>
<td>7159.0</td>
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</table>

* All reported computational times are in milliseconds

The results indicate that the improved SOM v2 [31] and the herein proposed GSOA are far the fastest solvers for the OP. However, the traditional CGW heuristic [52] provides the best results. On the other hand, the 4-phase heuristic [51] provides in some cases worse solution than the unsupervised learning based approaches and overall both SOM and GSOA approaches can be considered competitive. Regarding the comparison of the proposed GSOA to the previous SOM-based approaches, the overall solution quality is competitive with the SOM v2. Based on the statistical evaluation of the average sum of the collected rewards among the performed trials using the t-test with the significance level of 0.05, the SOM v2 provides statistically significant better solutions for the Set 66 with T_{\text{max}} \in \{60, 120\} and the GSOA provides better results for the Set 66 with T_{\text{max}} \in \{45, 85\}, which are highlighted in Table 2. In all other cases, differences in the solutions quality for both approaches (the SOM v2 and the herein proposed GSOA) are not statistically significant. However, the main expectations are in solutions of the Close Enough OP (CEOP) for which the results are reported in the following section.

5.3. **GSOA in the Close Enough Orienteering Problem**

The performance of the GSOA in the CEOP has been evaluated in the same problems as the comparison of the SOM v1 and SOM v2 reported in [31], i.e., in the Set 64 with T_{\text{max}} = 45 and Set 66 with T_{\text{max}} = 60, and \( \delta \in \{0.0, 0.5, 1.0, 1.5, 2.0\} \). Besides, the newly introduced Set 130 with T_{\text{max}} = 200 and T_{\text{max}} = 300 and \( \delta \in \{0, 1, 2, 3, 4\} \) is considered to show the performance of the CEOP solvers in larger instances. The average values of the solution cost \( R \) computed as the sum of the collected rewards are presented in Fig. 12a, Fig. 12b, and Fig. 13.
Figure 12: The average sums of the collected rewards in the OP Set 64 and Set 66 scenarios for the selected $T_{\text{max}}$ and the communication range $\delta$. The previous SOM-based approaches are denoted SOM v1 [30] and SOM v2 [31].

Figure 13: The average sums of the collected rewards in the OP Set 130 scenarios with the travel budget $T_{\text{max}} \in \{200, 300\}$ and the communication range $\delta$. The previous SOM-based approaches are denoted SOM v1 [30] and SOM v2 [31].
Overall, the proposed GSOA provides the best solutions and noticeably improves the performance of unsupervised learning based solution of the CEOP. It seems it solves the worse performance of the SOM v2 than SOM v1 in the Set 66 with $\delta = 0.5$, and it provides stable performance with the expected increase of the collected rewards with increasing the communication range $\delta$. The computational requirements are similar to the SOM v2 as in the solution of the OP, and therefore, a presentation of detail results is omitted.

5.4. GSOA in the CEOP with Spatial Correlation

The proposed GSOA is the first solution of the CEOP with spatial correlations, and therefore, the performance of the solver is studied for all the travel budgets of the problems Set 64, Set 66, and Set 130. For the instances of the Set 64 and Set 66, the spatial correlations are modeled for the rewards radius $\xi = 0.5$, which can be compared with the mutual distance of the sensor locations in Fig. 9 where the communication range $\delta = 0.5$ is visualized.
Table 3: Performance of the Proposed GSOA solver for the OP in Set 130

<table>
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<tr>
<th>$T_{\text{max}}$</th>
<th>$R_{\text{ref}}$</th>
<th>4-phase [51]</th>
<th>SOM v1 [30]</th>
<th>SOM v2 [31]</th>
<th>Proposed GSOA</th>
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<td>ARPE</td>
<td>$T_{\text{CPU}}$</td>
<td>RPE</td>
<td>ARPE</td>
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<td>5.62</td>
<td>47 137.0</td>
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</table>

*All reported computational times are in milliseconds

The correlation radius $\chi$ is selected from the set $\chi \in \{0, 1, 2\}$ and the communication radius $\delta$ is one of the three possible values $\delta \in \{0.0, 0.5, 1.0\}$. For the instances of the Set 130, a longer reward radius $\xi = 2.5$ is considered because of the large scale problem. The correlation radius $\chi$ and the communication radius $\delta$ are selected from the set $\chi \in \{0, 1, 2\}$ and $\delta \in \{0.0, 1.0\}$, respectively. Detail results are depicted in Table 4, Table 5, and Table 6, where it can be noticed the maximal rewards $R = 1344.0$, $R = 1680.0$, $R = 3609.0$ for the Set 64, Set 66, and Set 130 respectively, are achieved for lower budgets because of increasing communication radius $\delta$ as well as exploiting the spatial correlations for increasing correlation radius $\chi$.

Overall results are depicted in Fig. 14a and Fig. 14b. Selected best found solutions are visualized in Fig. 17, Fig. 18, Fig. 19, Fig. 20, Fig. 21, and Fig. 22.

Figure 14: The sums of the collected rewards in the OP instances of the Set 64 and Set 66 with the travel budget $T_{\text{max}}$, correlation radius $\chi$, and communication range $\delta$. The collected rewards are shown as the percentage of the total rewards in the scenario.

An overview of the solution improvement is shown in Fig. 14a for the Set 64 and selected $T_{\text{max}} = 20$ and $T_{\text{max}} = 45$. In Fig. 14b, the overview of the solution cost is presented for the Set 66 and $T_{\text{max}} = 60$ and $T_{\text{max}} = 85$. Both plots support the idea of improving the solution cost by considering not only non-zero communication radius $\delta$ but also the correlation radius $\chi$. 

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The computational requirements of the GSOA are very low, and solutions are found in tens of milliseconds. Therefrom sensors providing data with decreased information gain because of the collected data from the nearby sensors. The most supportive results are presented for the CEOP with spatial correlations, where the solution can benefit in saving the travel cost by retrieving data within the communication range and avoiding data collection from sensors providing data with decreased information gain because of the collected data from the nearby sensors. The computational requirements of the GSOA are very low, and solutions are found in tens of milliseconds. Therefore a relatively high number of learning epochs $i_{\text{max}} = 500$ can be considered without a noticeable increase in the computational time. On the other hand, the current low computational requirements motivate for employing active perception [39], while it can save the computational power for demanding image processing or localization.

5.5. Discussion

Regarding the presented results, the proposed GSOA for the CEPCTSP and CEOP seems to be a vital alternative to the combinatorial approaches and also to the previous SOM-based unsupervised learning methods. Although the performance in solving the standard OP seems to be a bit worse than the previous SOM v2 [31], the GSOA provides statistically competitive results. Besides, the proposed GSOA provides better results in solving the CEOP. The most supportive results are presented for the CEOP with spatial correlations, where the solution can benefit in saving the travel cost by retrieving data within the communication range and avoiding data collection from sensors providing data with decreased information gain because of the collected data from the nearby sensors.
Figure 17: Selected best found solutions of the CEOP Set 64 scenarios with $T_{\text{max}} = 20$, the communication radius $\delta$, and correlation radius $\chi$.

(a) $T_{\text{max}} = 20$, $\delta = 0.0$, $\chi = 0$, $R = 294$
(b) $T_{\text{max}} = 20$, $\delta = 0.0$, $\chi = 1$, $R = 340$
(c) $T_{\text{max}} = 20$, $\delta = 1.0$, $\chi = 2$, $R = 927$

Figure 18: Selected best found solutions of the CEOP Set 64 scenarios with $T_{\text{max}} = 45$, the communication radius $\delta$, and correlation radius $\chi$.

(a) $T_{\text{max}} = 45$, $\delta = 0.0$, $\chi = 0$, $R = 792$
(b) $T_{\text{max}} = 45$, $\delta = 0.5$, $\chi = 0$, $R = 1134$
(c) $T_{\text{max}} = 45$, $\delta = 1.0$, $\chi = 0$, $R = 1344$

(d) $T_{\text{max}} = 45$, $\delta = 0.0$, $\chi = 1$, $R = 913$
(e) $T_{\text{max}} = 45$, $\delta = 0.5$, $\chi = 1$, $R = 1189$
(f) $T_{\text{max}} = 45$, $\delta = 0.0$, $\chi = 2$, $R = 1338$

other local optimization strategies, e.g., such as VNS [58], to improve the solution, especially in the solution of the standard OP.
Figure 19: Selected best found solutions of the CEOP Set 66 scenarios with $T_{\text{max}} = 60$, the communication radius $\delta$, and correlation radius $\chi$.

(a) $T_{\text{max}} = 85$, $\delta = 0.0$, $\chi = 2$, $R = 1277$
(b) $T_{\text{max}} = 85$, $\delta = 0.5$, $\chi = 2$, $R = 1423$
(c) $T_{\text{max}} = 85$, $\delta = 1.0$, $\chi = 2$, $R = 1656$

Figure 20: Selected best found solutions of the CEOP Set 66 scenarios with $T_{\text{max}} = 85$, the communication radius $\delta$, and correlation radius $\chi$.

(a) $T_{\text{max}} = 85$, $\delta = 0.0$, $\chi = 2$, $R = 1593$
(b) $T_{\text{max}} = 85$, $\delta = 0.5$, $\chi = 2$, $R = 1672$
(c) $T_{\text{max}} = 85$, $\delta = 1.0$, $\chi = 0$, $R = 1680$
Figure 21: Selected best found solutions of the CEOP Set 130 scenarios with $T_{\text{max}} = 200$, the communication radius $\delta$, and correlation radius $\chi$. The initial and terminal locations are very close and they are the right most locations, approximately in the middle of the locations (vertically).

Figure 22: Selected best found solutions of the CEOP Set 130 scenarios with $T_{\text{max}} = 300$, the communication radius $\delta$, and correlation radius $\chi$. The initial and terminal locations are very close and they are the right most locations, approximately in the middle of the locations (vertically).
Table 4: Performance of the proposed GSOA in the CEOP with spatially correlated measurements in the Set 64 problems

<table>
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<th>$R$ for $\chi = 1$</th>
<th>$R$ for $\chi = 2$</th>
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Table 5: Performance of the proposed GSOA in the CEOP with spatially correlated measurements in the Set 66 problems

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<td>( \delta = 0.5 )</td>
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<td>381 429 529</td>
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</tbody>
</table>
Table 6: Performance of the proposed GSOA in the CEOP with spatially correlated measurements in the Set 130 problems

<table>
<thead>
<tr>
<th>Problem, $T_{\text{max}}$</th>
<th>$R$ for $\chi = 0$</th>
<th>$R$ for $\chi = 1$</th>
<th>$R$ for $\chi = 2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\delta = 0$</td>
<td>$\delta = 1$</td>
<td>$\delta = 2$</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 50$</td>
<td>375</td>
<td>462</td>
<td>530</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 100$</td>
<td>839</td>
<td>1092</td>
<td>1254</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 150$</td>
<td>1185</td>
<td>1527</td>
<td>1769</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 200$</td>
<td>1545</td>
<td>2113</td>
<td>2408</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 250$</td>
<td>2042</td>
<td>2776</td>
<td>3207</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 300$</td>
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<td>3389</td>
<td>3609</td>
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<td>Set 130, $T_{\text{max}} = 350$</td>
<td>3036</td>
<td>3609</td>
<td>3609</td>
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<tr>
<td>Set 130, $T_{\text{max}} = 400$</td>
<td>3503</td>
<td>3609</td>
<td>3609</td>
</tr>
<tr>
<td>Set 130, $T_{\text{max}} = 410$</td>
<td>3584</td>
<td>3609</td>
<td>3609</td>
</tr>
</tbody>
</table>
6. Conclusion

The herein proposed GSOA-based solution for solving the Close Enough Prize-Collecting Traveling Salesman Problem and Close Enough Orienteering Problem (both with spatial correlations) represents a unifying approach for data collection planning where it is requested to determine a cost-efficient path to retrieve the most rewarding sensor measurements from a set of pre-deployed sensors. The proposed solution allows exploiting not only the remote reading of the data from the sensors but also possible spatial correlations where data from one sensor includes information about the measurements from nearby locations. The proposed GSOA solver has low computational requirements and based on the previous comparison of the SOM-based solvers with combinatorial heuristics in the solution of the PCTSP, it provides better results. Moreover, the GSOA improves performance in a solution of the CEOP that is a suitable formulation of the data collection missions with the limited travel budget, which better fits the limitations of real robotic platforms. The reported results support the feasibility of the proposed approach and the current computational requirements of the GSOA technique provides a groundwork for further improvements of the solution quality or generalization for data collection planning for a team of vehicles.

On the other hand, the utilized distant based spatial correlations model is a general model that is easy to compute, and a more complex relation of the spatiotemporal field can be more demanding. Therefore, one of the planned future work is to employ the proposed GSOA in mission scenarios with a more complex model of the spatiotemporal field, where the studied phenomena are not static, and the rewards vary in time.

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7. References


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